## RELATIONS \& FUNCTIONS Worksheet

1. 



Using the vertical line test, determine if the graph above shows a relation, a function, both a relation and a function, or neither a relation nor a function.A. neither a relation nor a functionB. relation onlyC. both a relation and a functionD. function only
2. Which of these graphs represents a function?




A. Z
B. X
C. W
D. Y
3. Which of these t-tables represents a function?

| $x$ | $f(x)$ | $x$ | $f(x)$ | $\chi$ | $f(x)$ | $x$ | $f(x)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5 | -1 | 2 | -2 | -2 | 0 | -2 | 0 |
| 3 | 0 | 0 | 0 | 0 | 2 | 0 | 2 |
| 5 | 1 | 2 | 2 | 2 | 0 | 2 | 0 |
| 7 | 2 | 8 | 4 | 1 | 1.7 | 0 | -2 |
| W. |  | X. |  | Y. |  | Z. |  |

A. W
B. Y
C. Z
D. X
4. Which of these graphs represents a function?




A. Z
B. W
C. X
D. Y
5. Which of the following relations describes a function?A. $\{(0,0),(0,2),(2,0),(2,2)\}$
B. $\{(2,2),(2,3),(3,2),(3,3)\}$
C. $\{(2,-1),(2,1),(3,-1),(3,1)\}$D. $\{(-2,-3),(-3,-2),(2,3),(3,2)\}$
6. Do the ordered pairs below represent a relation, a function, both a relation and a function, or neither a relation nor a function?

$$
(-2,-1),(1,-4),(7,-10),(8,-11)
$$

A. neither a relation nor a functionB. both a relation and a function
C. relation onlyD. function only
7.


Determine whether this picture is an example of a function, relation, function and relation, or neither relation nor function.
A. function and relationB. function only
C. relation onlyD. neither function nor relation
8. Which relation diagram represents a function?
A. ZB. XC. WD. Y
9. Which of the following relations describes a function?A. $\{(2,2),(3,2),(4,2),(5,2)\}$
B. $\{(-2,0),(0,-2),(0,2),(2,0)\}$
C. $\{(0,0),(2,-2),(2,2),(3,3)\}$D. $\{(2,3),(2,4),(2,5),(2,6)\}$
10. Which of these graphs represents a function?




A. Y
B. X
C. Z
D. W
11. Which relation diagram represents a function?
A. WB. XC. YD. Z
12. Which of the following relations describes a function?A. $\{(0,0),(1,-1),(1,1),(2,2)\}$
B. $\{(-2,2),(-1,-1),(-1,1),(0,0)\}$C. $\{(-1,0),(0,1),(1,0),(0,-1)\}$
D. $\{(-2,2),(-1,1),(1,1),(2,2)\}$
13. Which of these mappings is a function?

W.

X.

Y.

Z.
$\bigcirc$
A. WB. ZC. XD. Y
14. Which of these graphs represents a function?




A. XB. WC. YD. Z
15. Which of these mappings is a function?

W.

X.

Y.

Z.A. WB. Y
C. XD. Z
16. Which of the following represents a relation and not a function?

O

A. | $x$ | - | -6 | - | 1 |
| :---: | :---: | :---: | :---: | :---: |
| $y$ | 34 | 32 | 40 | 34 |B.

| $\boldsymbol{x}$ | - | -6 | -2 | 1 |
| :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{y}$ | 34 | 32 | 40 | 34 |C.


| $x$ | - | -6 | 6 | 12 |
| :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{y}$ | 34 | 32 | 40 | 34 |D. | $\boldsymbol{x}$ | 6 | -6 | 12 | - |
| :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{y}$ | 34 | 32 | 40 | 34 |

17. Think about the vertical line test and answer the following question. Would a vertical line be a relation, a function, both a relation and a function, or neither a relation nor a function?
A. function onlyB. both a relation and a function

○
C. neither a relation nor a function
D. relation only
18. Which of the following graphs is not a function?




Z.
A. YB. WC. Z
D. X
19. Which of these $t$-tables represents a function?

| $x$ | $f(x)$ |  | $x$ | $f(x)$ |  | $x$ | $f(x)$ |  | $x$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | -2 | 0 |  | -4 | 2 |  | -1 | -1 |  |

A. X
B. Z
C. YD. W
20. Which of the following relations describes a function?A. $\{(-3,9),(-2,4),(2,4),(3,9)\}$B. $\{(2,-2),(0,0),(2,2),(3,3)\}$

○. $\{(-2,0),(0,2),(2,0),(0,-2)\}$
D. $\{(9,-3),(4,-2),(4,2),(9,3)\}$
21. Which of the following graphs is not a function?
A. W, X, Y and ZB. ZC. Y and ZD. X and Y
22. Which relation diagram represents a function?
A. YB. WC. ZD. X
23.


Determine whether this picture is an example of a function, relation, function and relation, or neither relation nor function.
A. neither function nor relationB. relation only
C. function only
D. function and relation
24. Do the ordered pairs below represent a relation, a function, both a relation and a function, or neither a relation nor a function?
$(-4,-3),(1,-8),(-4,-14),(9,-16)$A. function onlyB. both a relation and a functionC. neither a relation nor a function
D. relation only
25. Which of these $t$-tables represents a function?

| $x$ | $f(x)$ | $x$ | $f(x)$ | $x$ | $f(x)$ | $x$ | $f(x)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | -1 | -1 | 0 | -1 | 3 | 3 | -1 |
| -1 | 0 | 0 | 1 | 0 | 1 | 1 | 0 |
| 0 | 1 | 1 | 0 | 1 | 3 | 3 | 1 |
| 3 | 2 | 0 | -1 | 2 | 5 | 5 | 2 |
| w. |  | X. |  | Y. |  | z. |  |

A. Y
B. Z
C. X
D. W

## Answers

1. B
2. D
3. B
4. D
5. D
6. B
7. C
8. C
9. A
10. A
11. A
12. D
13. B
14. D
15. D
16. A
17. D
18. C
19. C
20. A
21. B
22. D
23. B
24. D
25. A

## Explanations

1. A relation is a set of one or more ordered pairs.

A function is a relation in which each element of the domain is paired with EXACTLY one element of the range.

The Vertical Line Test: Given the graph of a relation, if a vertical line can be drawn that crosses the graph in more than one place, then the relation is not a function.

The graph does not pass the vertical line test; therefore, the graph is not a function, and it is a relation only.
2. Use the vertical line test to determine if the graphs represent a function.

The only graph given that passes the vertical line test is $\mathbf{Y}$.
3. A function maps each domain element to only one range element.

The t -table $\mathbf{Y}$ is the only table that does not show a domain element paired with two or more range elements.
4. Use the vertical line test to determine if the graphs represent a function.

The only graph given that passes the vertical line test is $\mathbf{Y}$.
5. A function is a set of ordered pairs such that for each domain element there is only one range element.

The set of ordered pairs $\{(-2,-3),(-3,-2),(2,3),(\mathbf{3}, \mathbf{2})\}$ is the only set that does not pair a domain element with two or more range elements.
6. A relation is a set of one or more ordered pairs.

A function is a relation in which each element of the domain is paired with EXACTLY one element of the range.

In this case, there is one $y$-coordinate for every $x$-coordinate.
The vertical line test can be used to determine this.
Therefore, it is both a relation and a function.
7. A relation is a set of one or more ordered pairs.

A function is a relation in which each element of the domain is paired with EXACTLY one element of the range.

The Vertical-Line Test: Given the graph of a relation, if a vertical line can be drawn that does not cross the graph in more than one place, it is a function.

Any vertical line drawn where $x>-4$ will cross the graph in more than one place.
Therefore, the graph is not a function, it is a relation only.
8. For a relation to be a function, each input value can only correspond to one output value. The relation diagram where each input value has exactly one arrow drawn to an output value will represent a function.

Therefore, diagram $\mathbf{W}$ represents a function.
9. A function is a set of ordered pairs such that for each domain element there is only one range element.

The set of ordered pairs $\{(\mathbf{2}, \mathbf{2}),(\mathbf{3}, \mathbf{2}),(\mathbf{4}, \mathbf{2}),(\mathbf{5}, \mathbf{2})\}$ is the only set that does not pair a domain element with two or more range elements.
10. Use the vertical line test to determine if the graphs represent a function.

The only graph given that passes the vertical line test is $\mathbf{Y}$.
11. For a relation to be a function, each input value can only correspond to one output value. The relation diagram where each input value has exactly one arrow drawn to an output value will represent a function.

Therefore, diagram $\mathbf{W}$ represents a function.
12. A function is a set of ordered pairs such that for each domain element there is only one range element.

The set of ordered pairs $\{(\mathbf{- 2}, \mathbf{2}),(\mathbf{- 1}, \mathbf{1}),(\mathbf{1}, \mathbf{1}),(\mathbf{2}, \mathbf{2})\}$ is the only set that does not pair a domain element with two or more range elements.
13. A function maps each domain element to only one range element.

The only mapping that does not map a domain element to two or more range elements is $\mathbf{Z}$.
14. Use the vertical line test to determine if the graphs represent a function.

The only graph given that passes the vertical line test is $\mathbf{Z}$.
15. A function maps each domain element to only one range element.

The only mapping that does not map a domain element to two or more range elements is $\mathbf{Z}$.
16. A relation is a set of one or more ordered pairs.

A function is a relation in which each element of the domain is paired with EXACTLY one element of the range.

In the table below, there are two $y$-coordinates for the $x$-coordinate -10 . Therefore, it is a relation only and not a function.

| $\boldsymbol{x}$ | - | -6 | - | 10 |
| :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{y}$ | 34 | 32 | 10 | 40 |

17. A relation is a set of one or more ordered pairs.

A function is a relation in which each element of the domain is paired with EXACTLY one element of the range.

The Vertical-Line Test: Given the graph of a relation, if a vertical line can be drawn that does not cross any of the graphs in more than one place, it is a function.

If the relation being tested is a vertical line, then any $x$ in the domain of the relation (which there would be only one) will correspond with every $y$ of the range (an infinite number of points).

So, a vertical line can be drawn that crosses the graph in more than one place (the vertical line itself).
Therefore, a vertical line is not a function, and it is a relation only.
18. A relation is a set of one or more ordered pairs.

A function is a relation in which each element of the domain is paired with EXACTLY one element of the range.

The Vertical Line Test: Given the graph of a relation, if a vertical line can be drawn that crosses the graph in more than one place, then the relation is not a function.

Therefore, graph $\mathbf{Z}$ is not a function.
19. A function maps each domain element to only one range element.

The t-table $\mathbf{Y}$ is the only table that does not show a domain element paired with two or more range elements.
20. A function is a set of ordered pairs such that for each domain element there is only one range element.

The set of ordered pairs $\{(\mathbf{- 3}, \mathbf{9}),(\mathbf{- 2}, \mathbf{4}),(\mathbf{2}, \mathbf{4}),(\mathbf{3}, \mathbf{9})\}$ is the only set that does not pair a domain element with two or more range elements.
21. A relation is a set of one or more ordered pairs.

A function is a relation in which each element of the domain is paired with EXACTLY one element of the range.

The Vertical-Line Test: Given the graph of a relation, if a vertical line can be drawn that does not cross any of the graphs in more than one place, it is a function.

Therefore, $\mathbf{Z}$ is not a function.
22. For a relation to be a function, each input value can only correspond to one output value. The relation diagram where each input value has exactly one arrow drawn to an output value will represent a function.

Therefore, diagram $\mathbf{X}$ represents a function.
23. A relation is a set of one or more ordered pairs.

A function is a relation in which each element of the domain is paired with EXACTLY one element of the range.

The Vertical Line Test: Given the graph of a relation, if a vertical line can be drawn that crosses the graph in more than one place, then the relation is not a function.

Since the graph does not pass the vertical line test, it is not a function, it is a relation only.
24. A relation is a set of one or more ordered pairs.

A function is a relation in which each element of the domain is paired with EXACTLY one element of the range.

There are two $y$-coordinates (range element) when $x=-4$.
Therefore, it is a relation only.
25. A function maps each domain element to only one range element.

The t-table $\mathbf{Y}$ is the only table that does not show a domain element paired with two or more range elements.

